

Seat No.: _____

Enrolment No. _____

GUJARAT TECHNOLOGICAL UNIVERSITY

BE - SEMESTER-VIII (NEW) - EXAMINATION – SUMMER 2018

Subject Code: 2181911

Date: 30/04/2018

Subject Name: Finite Elements Method(Department Elective II)

Time: 10:30 AM to 01:00 PM

Total Marks: 70

Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) Can the FEM handle a wide range of problems, i.e., solve general PDEs? **03**
Enlist two advantages of FEM.
- (b) List four applications of FEM and computer programs used for the FEM. **04**
- (c) List and briefly describe the process of the Finite Element Method. **07**
- Q.2** (a) What are the characteristics of shape function? Why polynomials are generally used as shape function? **03**
- (b) Draw three 2D and 3D types of finite element. **04**
- (c) Derive the Stiffness Matrix for a Spring Element. **07**

OR

- (c) (a) Formulate the global stiffness matrix and equations for solution of the unknown global displacement and forces. The spring constants for the elements are k_1 ; k_2 , and k_3 ; P is an applied force at node 2. **07**
- (b) Using the direct stiffness method, formulate the same global stiffness matrix and equation as in part (a).

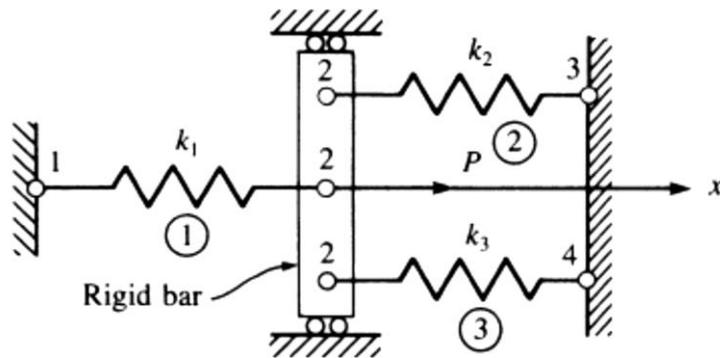


Figure 1

- Q.3** (a) Distinguish between essential boundary conditions and natural boundary conditions. Give their examples. **03**
- (b) Discuss the penalty approach for FEM. **04**
- (c) A tapered bar 1200 mm long, having cross-sectional area 450 mm^2 at one end and 150 mm^2 at other end is fixed at the larger end. It is subjected to an axial load of 35 kN. Calculate the stress on a model bar having three finite elements 400 mm long. Assume modulus of elasticity, $E = 2 \times 10^5 \text{ N/mm}^2$ circular cross section at both end. **07**

OR

- Q.3 (a)** For the loading system as shown in Figure 2, determine the element stiffness matrix and global stiffness matrix. Assume modulus of elasticity as $80 \times 10^3 \text{ N/mm}^2$ **03**

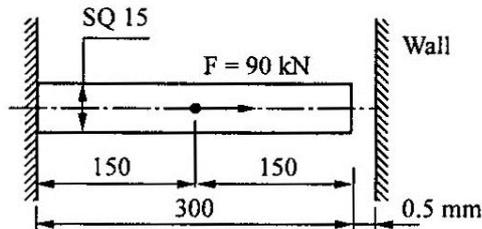


Figure 2

- (b)** For above Q. 3 (a) determine the displacements, stresses and support reaction using penalty approach. **04**
- (c)** Axial load $P = 300 \text{ kN}$ is applied at 20° C to the rod as shown in Figure 3. The temperature is then raised to 60° C . The coefficient of thermal expansion for Aluminium is 23×10^{-6} per $^\circ \text{ C}$ and Steel is 11.7×10^{-6} per $^\circ \text{ C}$. $A_{\text{Al}} = 900 \text{ mm}^2$, $A_{\text{Steel}} = 1200 \text{ mm}^2$, $E_{\text{Al}} = 70 \times 10^9 \text{ N/m}^2$, $E_{\text{Steel}} = 200 \times 10^9 \text{ N/m}^2$. Using FEM, Determine the nodal displacement and element stresses and the reaction forces at the supports. **07**

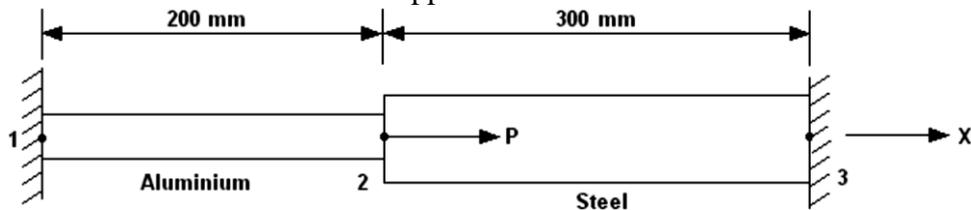


Figure 3

- Q.4 (a)** Write the shape function and stiffness matrix for one-dimensional finite element formulation of the fluid-flow problem. **03**
- (b)** Derive the element stiffness matrix of truss element and write the stress calculation formula for truss. **04**
- (c)** A three bar truss is shown in Figure 4. The modulus of elasticity of the material is $300 \times 10^3 \text{ N/mm}^2$. The area of the bar used for the truss is 60 mm^2 for all the elements. The length $L_1 = 750 \text{ mm}$ and $L_2 = 100 \text{ mm}$. The load $P = 20 \text{ kN}$ and $P_2 = 25 \text{ kN}$. Determine the element stiffness matrix for each element and the global stiffness matrix. **07**

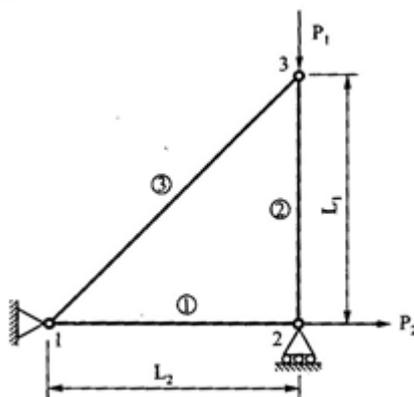


Figure 4

OR

- Q.4** (a) List out the application of axisymmetric elements. **03**
 (b) Discuss the terms “plain stress” and “plain strain” problems. **04**
 (c) Evaluate the stiffness matrix for the element shown in Figure 5. The coordinates are shown in units of inches. Assume plane stress conditions. Let $E = 30 \times 10^6$ psi, $\nu = 0.25$, and thickness $t = 1$ in. Assume the element nodal displacements have been determined to be $u_1 = 0$, $v_1 = 0.0025$ in., $u_2 = 0.0012$ in., $v_2 = 0$, $u_3 = 0$, and $v_3 = 0.0025$ in. Determine the element stresses. **07**

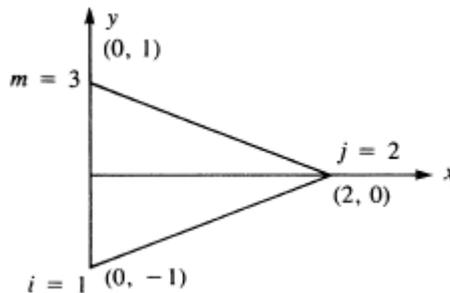


Figure 5 Plane stress element for stiffness matrix evaluation

- Q.5** (a) Write the point force, body force and surface traction force using natural coordinate system. **03**
 (b) Write the four shape function equations for a beam element. **04**
 (c) Using the direct stiffness method, solve the problem of the propped cantilever beam subjected to end load P in Figure 6. The beam is assumed to have constant EI and length $2L$. It is supported by a roller at mid length and is built in at the right end. Propped cantilever beam shown in below Figure 6 **07**

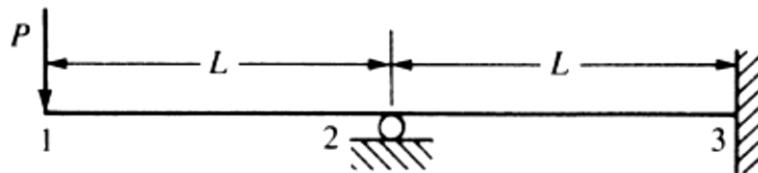


Figure 6

OR

- Q.5** (a) Write the consistent and lumped mass matrices for 1D element. **03**
 (b) List out applications of the axisymmetric elements. **04**
 (c) For the smooth pipe shown discretized in Figure 7 with uniform cross section of 1 in^2 , determine the flow velocities at the center and right end, knowing the velocity at the left end is $v_x = 2 \text{ in./s}$. **07**

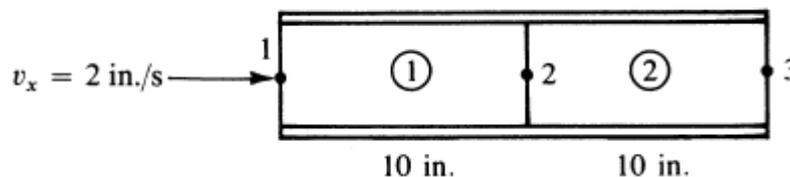


Figure 7 Discretized pipe for fluid-flow problem
